Claims

- A method of calculating a modification of a geometrical shape, comprising the steps of: 1. 1 defining on a multi-dimensional space an array of values representing a geometrical 2 shape; 3 selecting a modification function that represents a desired modification to be applied to 4 the geometrical shape; 5 applying an inverse function of the modification function to the array of values to produce 6 a modified array; and 7 deducing from the modified array a modification of the geometrical shape that would 8 result from a direct application of the modification function to the array. 9 The method of claim 1, further comprising the step of applying the deduced modification 2. to the array. The method of claim 1, further comprising displaying to a user the modification of the 3. geometrical shape that would result from a direct application of the modification function to the array. The method of claim 1, wherein the step of deducing from the modified array a -1 4. modification further comprises the steps of: 2 retrieving an array value from the modified array; and 3 applying the array value from the modified array at a location in the array representing the 4 geometrical shape. 5
 - 1 5. The method of claim 1, wherein the modification function comprises a soft-edged deformation.
 - 1 6. The method of claim 1, wherein the modification function is applied from a selected one 2 of a first side and a second side of the geometrical shape.

- The method of claim 1, further comprising applying the modification function by 1 7.
- manipulation of a virtual tool. 2
- The method of claim 7, wherein the geometrical shape is displaced away from the virtual 8. 1
- 2 tool.
- The method of claim 7, wherein the geometrical shape is displaced toward the virtual 1 9.
- 2 tool.
- The method of claim 9, wherein the modification of the geometrical shape is substantially 1 10. a convex hump.
 - The method of claim 9, wherein the modification of the geometrical shape is substantially 11. a concave spiked protuberance.
 - The method of claim 1, wherein the modification function comprises a force field 12. consistent with a tool of arbitrary shape.
 - The method of claim 1, wherein the modification function comprises translational 13.
 - 2 displacement.

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- The method of claim 1, wherein the modification function comprises rotational 1 14.
- 2 displacement.
- The method of claim 1, wherein the modification function comprises a selected one of a 15. 1
- displacement function, a smoothing function, a warping function, a volumetric interference, an 2
- areal interference, a result of a simulation, a data re-fitting, and a force. 3
- The method of claim 1, wherein the modification function is represented as a non-linear 16. 1
- mathematical function. 2

1	17.	The method of claim 1, further comprising the steps of:
2		selecting a second modification function;
3		applying an inverse function of the second modification function to the modified array to
4		produce a twice-modified array; and
5		deducing from the twice-modified array a modification of the geometrical shape that
6		would result from an application of the modification function to the array followed by
7		an application of the second modification function to the once-modified array.
1	18.	The method of claim 1, wherein the modification comprises applying a constraint so as to
	control a magnitude of a change of the geometrical shape.	
	19.	The method of claim 18, wherein applying the constraint prevents at least one point of the
L 2	geometrical shape from moving in response to the application of the inverse function of the	
54 = 3 	modi	fication function.
: w 	20.	The method of claim 1, wherein the modification comprises applying a surface texture to
	the go	eometrical shape.
1	21.	A system for calculating a modification of a geometrical shape, comprising:
2		a generation module that defines on a multi-dimensional space an array of values
3		representing a geometrical shape;
4		a selection module that provides a modification function representing a desired
5		modification to be applied to the geometrical shape;
6		a transformation module that applies an inverse function of the modification function to
7		the array of values to produce a modified array; and
8		a calculation module that deduces from the modified array a modification of the
9		geometrical shape that would result from a direct application of the modification
10		function to the array.

- 1 22. The system of claim 21, further comprising a modification module that applies the
- 2 deduced modification to the array.
- 1 23. The system of claim 21, further comprising a display module that displays to a user the
- 2 modification of the geometrical shape that would result from a direct application of the
- 3 modification function to the array.

- 1 24. The system of claim 21, wherein the calculation module further comprises:
- a module that retrieves an array value from the modified array; and
 - a module that applies the array value from the modified array at a location in the array representing the geometrical shape.
 - 25. The system of claim 21, wherein the modification function comprises a soft-edged deformation.
 - 26. The system of claim 21, wherein the modification function is applied from a selected one of a first side and a second side of the geometrical shape.
 - 27. The system of claim 21, further comprising a module that applies the modification
- 2 function by manipulation of a virtual tool.
- 1 28. The system of claim 27, wherein manipulation of a virtual tool displaces the geometrical
- 2 shape away from the virtual tool.
- 1 29. The system of claim 27, wherein manipulation of a virtual tool displaces the geometrical
- 2 shape toward the virtual tool.
- 1 30. The system of claim 29, wherein the modification of the geometrical shape is
- 2 substantially a convex hump.

- 1 31. The system of claim 29, wherein the modification of the geometrical shape is
- 2 substantially a concave spiked protuberance.
- 1 32. The system of claim 21, wherein the modification function comprises a force field
- 2 consistent with a tool of arbitrary shape.
- 1 33. The system of claim 21, wherein the modification function comprises translational
- 2 displacement.

- 34. The system of claim 21, wherein the modification function comprises rotational displacement.
- 35. The system of claim 21, wherein the modification function comprises a selected one of a displacement function, a smoothing function, a warping function, a volumetric interference, an areal interference, a result of a simulation, a data re-fitting, and a force.
- 36. The system of claim 21, wherein the modification function is represented as a non-linear mathematical function.
- 1 37. The system of claim 21, further comprising:
- 2 a selection module that selects a second modification function;
- a transformation module that applies an inverse function of the second modification
- function to the modified array to produce a twice-modified array; and
- a calculation module that deduces from the twice-modified array a modification of the
- 6 geometrical shape that would result from an application of the modification function to
- 7 the array followed by an application of the second modification function to the once-
- 8 modified array.
- 1 38. The system of claim 21, wherein the modification comprises applying a constraint so as
- 2 to control a magnitude of a change of the geometrical shape.

- 1 39. The system of claim 38, wherein the module that applies the constraint prevents at least
- 2 one point of the geometrical shape from moving in response to the application of the inverse
- 3 function of the modification function.
- 1 40. The system of claim 21, wherein the modification comprises applying a surface texture to
- 2 the geometrical shape.